

- \_\_\_\_\_ 1.) How many positive integers are equal to the number of letters in the English spelling of the number? (For example, the word "fifteen" has only 7 letters, so it would not be counted as one of the words we are looking for). Do not count spaces or special characters... only letters!
- \_\_\_\_\_ 2.) Initially, a certain state was considering license plates with one capital letter followed by five single-digit integers (0 thru 9). However, they ultimately decided to go with two capital letters followed by four single-digit integers. What is the positive difference in the number of possible plates offered by the two options?
- \_\_\_\_\_ 3.) How many of the 7<sup>th</sup> roots of  $-1$  lie in the 1<sup>st</sup> Quadrant of the complex plane?
- \_\_\_\_\_ 4.) What is the exact value of  $\sin\left(\frac{1819\pi}{6}\right)$ ?
- \_\_\_\_\_ 5.) A cube of side length 10 is inscribed in a cylinder. What is the volume of the cylinder?
- \_\_\_\_\_ 6.) Omar gives  $\frac{1}{4}$  of his gumballs to Manuel,  $\frac{1}{5}$  of the remaining gumballs to Rajesh, then  $\frac{1}{6}$  of the remaining gumballs to Dietrich. If he never had to split a gumball into parts during any of this process, what is the smallest number of gumballs with which he could have started?
- \_\_\_\_\_ 7.) Write the solution to the system as an ordered pair:  
 $7x + 3y = 35$  and  $4x - 5y = -27$ .
- \_\_\_\_\_ 8.) When  $x^4 - 5x^3 + kx^2 + 7x - 5$  is divided by  $x + 1$ , the remainder is 42. What is the value of  $k$ ?
- \_\_\_\_\_ 9.) Find the positive value of  $x$  so that the determinant of the given matrix has a value of 30.  $\begin{bmatrix} 2 & 3 & x \\ 4 & x & 2 \\ 1 & 2 & x \end{bmatrix}$
- \_\_\_\_\_ 10.) 50% of the 24 students in Mrs. A's class and 40% of the 25 students in Mrs. B's class are boys. In Mrs. C's class, the 6 boys represent 30% of the students. To the nearest integer, what percent of all students in the 3 classes are boys?
- \_\_\_\_\_ 11.) How many solutions does the equation  $\sin(x) = \frac{1}{6}x$  have?
- \_\_\_\_\_ 12.) Fifteen distinguishable runners run a race. How many ways are there to award gold, silver, and bronze medals (one of each)?
- \_\_\_\_\_ 13.) The set of possible values of  $k$ , for which the lines  $y = \frac{3}{4}x - 3$  and  $y = kx - 5$  intersect in the first Quadrant, can be expressed as the open interval  $(a, b)$ . What is the value of  $a + b$ ?
- \_\_\_\_\_ 14.) When 4 fair coins are flipped, what is the probability that 2 are heads up and 2 are heads down?
- \_\_\_\_\_ 15.) John made 85, 76, 78, and 72 on his first 4 tests. What score does he need to make on his fifth test in order to have an average of exactly 80?
- \_\_\_\_\_ 16.) What is the sum of ALL of the solutions to the equation:  
 $(2x^2 - 5x + 6)(x^2 - 7x + 4) = 0$
- \_\_\_\_\_ 17.) Find the period of the function  $f(x) = 3 \cos\left(5x - \frac{\pi}{2}\right) + 4 \tan(2x - \pi)$ .
- \_\_\_\_\_ 18.) Calculate  $(977)(1023)$ .
- \_\_\_\_\_ 19.) What is the remainder when  $11^7$  is divided by 1000?
- \_\_\_\_\_ 20.) How many non-congruent rectangular prisms have positive integer side lengths and a volume of 24?
- \_\_\_\_\_ 21.) What is the distance between the points  $(-12, 4)$  and  $(6, -8)$  in simplest radical form?
- \_\_\_\_\_ 22.) Find:  $\lim_{x \rightarrow 2} \frac{x^3 - 4x^2 + x + 6}{x^2 - 3x + 2}$ .
- \_\_\_\_\_ 23.) Find the  $x$ -coordinate of the  $x$ -intercept of the line  $y = \frac{-3}{2}x + 8$ .
- \_\_\_\_\_ 24.) Find the area enclosed by the ellipse given by the equation:  $\frac{(x-4)^2}{64} + \frac{(y+3)^2}{16} = 2$ .
- \_\_\_\_\_ 25.) A particular regular polygon is such that each interior angle is 8 times the degree measure of each exterior angle. How many diagonals does this regular polygon have?